

## **Syllabus: Algebra Preliminary Examination 06/2022**

### **Topics which may be covered include:**

Groups: group homomorphisms, quotient groups, isomorphism theorems, group actions, direct and semi-direct products, fundamental theorem of finitely generated abelian groups

Rings and fields: ideals, ring homomorphisms, quotient rings, isomorphism theorems, fields of fractions, Chinese remainder theorem, Euclidean domains, principal ideal domains, unique factorization domains, polynomial rings, finite fields

### **References to help prepare:**

Abstract Algebra by Dummit and Foote, 3rd edition:

Chapters 1-3

Sections 1-4 of Chapter 4

Chapter 5

Chapters 7-8

Sections 1-5 of Chapter 9

Also, you should know basic results about finite fields, including how to construct finite fields of all possible orders.